

Autonomous Flight Test of a Novel Non-conventional Biplane Micro Air Vehicle

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ABSTRACT

This paper presents detailed mathematical modeling, controller design, and flight test results for the autonomous mission of a non-conventional fixed wing biplane Micro Air Vehicle (MAV) called

24 “Skylark” having span and chord length within 150 mm. Although numerous fixed wing MAV
25 designs are reported in the open literature, a MAV’s reliable autonomous flight is still a challenge.
26 The primary difficulties in performing the autonomous mission of fixed wing MAV are system
27 integration within the weight and power budget, CG management, and flight controller design for
28 fast dynamics. In this paper, the key challenges are addressed by using the higher payload capacity
29 of “Skylark”, suitable selection and design of avionics components, and design of controller after
30 detailed development of the mathematical model, including the additional effect of propeller wash
31 and motor counter torque. Autonomous flight test is successfully demonstrated after the validation
32 of algorithms and software architecture through nonlinear six-dof simulation. The detailed design
33 and development approach will increase MAV’s performance and reliability in civil and military
34 applications.

35 **INTRODUCTION**

36 MAVs’ importance for difficult and dangerous tasks in civilian and military applications is
37 increasing day by day. The era of MAVs officially began following the launch of the “Micro
38 Air Vehicle” program by DARPA in 1997. Unmanned air vehicle whose maximum dimension is
39 less than 150 mm and velocity around 10-20 m/s is generally classified as MAV (McMichael and
40 Francis 1997). Fixed wing MAV outperforms other MAVs when the mission requirement involves
41 high speed, long endurance, and high payload carrying capacity. Design and development issues
42 related to fixed wing Micro Air vehicle is reported in various literature (Mueller et al. 2000; Wood
43 et al. 2007; Michelson 2010; Moschetta 2014; Pipenberg and Maughmer 2015; Cai et al. 2014;
44 Phan and Park 2020; Hassanalian and Abdelkefi 2017); however, outdoor flight tests results are
45 reported in few cases such as SPOT (Hwang et al. 2002), Black Widow (Grasmeyer and Keennon
46 2001), Microbeacon (Suraj et al. 2013), KH2013A (Kandath et al. 2018). They are designed with
47 capabilities of remote-controlled flight or stabilized flight. Black Widow is capable of altitude hold,
48 airspeed hold, heading hold; KH2013A is capable of stabilized flight. Autonomous flight tests of
49 fixed wing small UAVs having size more than 150 mm is reported in literature; for example, with
50 12 inch MAV (Platanitis and Shkarayev 2005), 27 cm MAV (Aboelegg et al. 2020), 30 cm MAV

51 (Albertani et al. 2005), 49 cm wingspan (Mohamed et al. 2016), (Zhao et al. 2015). However, a
52 MAV having capabilities of autonomous navigation in an outdoor environment is not reported in
53 the open literature.

54 Progress on research and development of MAV of size 150 mm slowed down due to difficulty
55 in CG management of MAV with heavier payload and large avionics packages. The major issues
56 involved in performing autonomous flight tests are system integration within weight and power
57 budget, flight control design to handle the vehicle's fast dynamics (Michelson 2010). Different
58 controller structure is proposed for small-scale UAVs platforms using model predictive controller
59 (Campbell and Maciejowski 2009), switching PID controller (Zhu et al. 2007), dynamic inversion
60 based neural network (He and Wu 2008), μ -synthesis (Fujinaga et al. 2007), linear quadratic
61 gaussian controller (Lee et al. 2011). In case of MAVs, the controller design is reported using
62 robust output feedback (Harikumar et al. 2019), PID controller (Aboeizz et al. 2021). Important
63 challenges in developing a control algorithm for MAVs is due to the lack of high fidelity aerodynamic
64 models in the presence of propeller flow and motor counter-torque (Harikumar et al. 2016). The
65 detailed mathematical model also has to include effects of the propeller flow and motor-counter
66 torque as these have significant effects on the overall forces and moments acting on MAV.

67 In this paper, the autonomous flight of MAV is made possible through efficient hardware design
68 and software development after detailed mathematical modeling and analysis. In (Jana 2018),
69 the design of a non- conventional biplane MAV called "Skylark" to have better payload capacity
70 and higher static margin than the conventional MAVs is discussed. In this paper, the overall
71 system configuration of "Skylark" is finalized, and flight test results of an autonomous mission are
72 presented after detailed development of mathematical model and controller algorithm.

73 The autonomous navigation of "Skylark" is performed in the following stages. After the
74 finalization of aerodynamic configuration, the avionics components are selected such that it satisfies
75 the constraints of weight budget, power budget, and space budget. Then avionics components are
76 distributed inside the vehicle in such a way that it helps in obtaining favorable CG location and
77 balancing the counter-torque of the motor. Once every aspect of the vehicle configuration is decided,

78 a mathematical model of the plant is developed using the CAD modeling, wind tunnel test, and
79 standard empirical formula. As the contribution of propeller flow and motor counter-torque varies
80 mostly with the motor RPM, the aerodynamic forces acting on the "Skylark" due to these parameters
81 are modeled as a function of throttle RPM. The algorithms are designed after a detailed analysis
82 of the mathematical model and validated through six-dof simulation. Initially, the stabilized flight
83 is performed, where the control loop is handled through autopilot and guidance commands are
84 generated from a pilot. The feedback from the stabilized flight test observations is considered for
85 the adjustment of different system parameters. Finally, autonomous flight test is performed after
86 analysis of various stabilized flight test data.

87 The rest of the paper is described as follows: Detailed of the system design of "Skylark" MAV
88 for the autonomous mission is described in Section 2. In Section 3, the mathematical model of MAV
89 is developed, and analysis for algorithm design is performed. Controller and estimation design is
90 presented in Section 4. Six-dof simulation of MAV is discussed in Section 5. Autonomous flight
91 test results are presented in Section 6.

92 **SYSTEM DESIGN**

93 "Skylark" is a non-conventional biplane MAV designed to carry the payload for the vision
94 assisted autonomous navigation (Jana 2018; Jana et al. 2022). The important characteristics of
95 "Skylark" are that it has an optimum top wing, which helps in achieving higher payload capacity
96 as well as better stability margin. The span of the top and the bottom wing is kept the same;
97 however, the chord length of the top wing is designed as 60 % of the chord length of the bottom
98 wing considering the trade-off between payload carrying capacity and static longitudinal stability.
99 This unconventional design improves the lift co-efficient of the vehicle while shifting the overall
100 neutral point towards the trailing edge. "Skylark" has a higher range of allowable CG locations
101 beyond the center of pressure location of the bottom wing due to its non-conventional biplane
102 configuration. Passive techniques like asymmetric mass distribution about the forward axis and
103 vertical tail placement in propeller wash are used to help balance counter torque. Aerofoils selected
104 are of almost zero pitching moment and of high lift-coefficient. Control surfaces are designed

105 considering handling quality as per “MIL-F8785C”. In the Fig. 1, the fabricated model of the
106 MAV “Skylark” is shown. The important aerodynamic parameters of the “Skylark” are shown in
107 Table 1.

108 The aerodynamics responses of the MAV class of vehicles are highly sensitive to the motor-
109 propeller combination. The basic aerodynamic configuration of a MAV is arrived at considering
110 dummy payload and specific motor-propeller configuration. After the finalization of the aerody-
111 namic configuration, the avionics components are selected, considering the following points.

- 112 • Overall system should be equipped with the sensors and computational units such that it
113 can perform an autonomous mission.
- 114 • The weight of the components and the overall current consumption should be within the
115 weight and power budget.
- 116 • The components’ size and shape should be selected in an optimal manner such that compo-
117 nents can be placed within the allowable CG location without violating the requirement of
118 longitudinal stability.
- 119 • The components should be selected, such that the distribution of components will help in
120 balancing the motor counter-torque passively.

121 The components are selected iteratively while checking the above conditions. The important
122 components are the main controller unit, sensors, power module, telemetry module, GPS, electronic
123 speed controller (ESC), two nos. of battery, camera module, etc. The main sensors include
124 Altimeter, and 9-axis IMU consists of a gyroscope, accelerometer, magnetometer. Two batteries
125 are used to provide separate power to the motor and main controller unit. The main control unit is
126 designed based on a microprocessor so that the main autopilot tasks and the image processing tasks
127 can be performed simultaneously on a single board. The single board was necessary to satisfy the
128 constraints of weight, space, and CG location. The main controller unit, sensors, power module,
129 telemetry module, GPS, and other interfaces are combined in an autopilot board of 35 mm × 65
130 mm and weight of 16 grams. The weight of the structure, motor-propeller, 2S battery, 1S battery,

131 ESC, control servos, and camera module used are approximately 40 grams, 7 grams, 16 grams, 3
132 grams, 2 grams, 4 grams, and 5 grams respectively. The Airspeed sensor is not used in this case as
133 the output of this sensor fitted to MAV is found to be inaccurate. This is due to the fact that MAVs
134 are susceptible to gust as wind speed is comparable to MAV's velocity. Details of the avionics
135 hardware are given in Table 2. Figure 2 shows the details of avionics inside MAV.

136 The components are placed to obtain a favorable CG location, and the mass distribution is
137 made asymmetric to balance the counter-torque of the motor. Although torque balance can not be
138 maintained at different airspeeds, the asymmetric mass distribution will always help balance the
139 propeller torque throughout the speed regime". The components are placed as shown in Figure 3.
140 In this case, the propeller rotates in a clockwise motion (from the rear side), and in turn, due to
141 Newton's third law, the reaction force causing the MAV to rotate in an anticlockwise direction (roll
142 towards left). So, the right side of the MAV x-axis is made relatively heavier compared to another
143 side to balance the counter-torque passively. As shown in Fig. 2, the heavier 2S battery is placed on
144 the right side. The exact location of the components is decided after observations from the initial
145 flight tests. The autopilot is placed on the vibration dampening pad to reduce motor vibration's
146 effect on accelerometer output.

147 After finalizing the overall configuration, mathematical model, algorithms are developed for
148 autonomous missions and validated through simulations. A tentative flowchart for performing
149 autonomous navigation is shown in Fig. 4. The feedback connection implies that algorithm
150 design is performed iteratively after getting feedback from the simulations, stabilized flight, and
151 autonomous flights.

152 **PLANT MODELING AND ANALYSIS**

153 The system modeling aims to develop a mathematical model to capture the system dynamics
154 and describe the effects of the external forces on the system. Generally, for developing the
155 mathematical model of small-scale vehicles, first principle modeling, system identification, and
156 hybrid identification methods are used (Cai et al. 2014; Bogdanowicz et al. 2015). In first-principles
157 modeling, the system parameters are obtained based on the basic aircraft mechanics, XFLR analysis,

158 CAD modeling, wind tunnel test, and standard empirical results (Platanitis and Shkarayev 2005;
159 Harikumar et al. 2016; Phang et al. 2014; Wu et al. 2018); whereas, in system identification
160 methods, system parameters are estimated from the analysis of flight test results (Kumar et al. 2013;
161 Armanini et al. 2015; Burri et al. 2018). In the hybrid model, preliminary results of first principle
162 methods are further improved using the flight data (Armanini et al. 2016; Saderla et al. 2017).
163 System identification methods are suitable for the development of a linearized model about the
164 particular operating point; whereas, the first-principles approach or hybrid approach is preferred
165 for the development of the complete nonlinear model. Complete nonlinear modeling of the UAVs
166 is reported in the literature such as “Zaggi flying wing”, “Aerosonde” (Beard and McLain 2009)
167 etc. In the case of MAVs, aerodynamic parameters are estimated for 15 cm wingspan MAV from
168 wind tunnel test and empirical formula without incorporating the propeller flow (Kuo et al. 2007).
169 The contribution of propeller flow towards the system’s total lift and drag forces is reported in
170 (Harikumar et al. 2016; Null et al. 2005; Spoerry and Wong 2001). In this section, kinematics and
171 dynamics equations of the “Skylark” MAV is developed from the first principles approach.

172 MAV structure and its different components are modeled, and the moment of inertia for different
173 axis and planes is calculated using SOLIDWORKS software. The value of the moment of inertia
174 in xy plane and yz plane is not negligible due to the presence of top wing and asymmetric mass
175 distribution. The moment of inertia of the “Skylark” is calculated from the SOLIDWORKS software
176 and presented in Table 3, where J_{xx} , J_{yy} , J_{zz} are the moment of inertia of the MAV in x , y , z axis
177 and J_{xy} , J_{xz} , J_{yz} are the moment of inertia in xy , xz and yz plane respectively.

178 The fundamental kinematics and dynamics equations are available in the various literature
179 (Beard and McLain 2009). In this paper, the kinematics and dynamics equations are developed
180 along the similar lines. The following standard state variables are used in the modelling of MAV:
181 Position variables (p_n , p_e , p_d), component of inertial linear velocities along body frame (u , v , w),
182 attitudes (ϕ , θ , ψ) and angular rates (p , q , r).

183 The kinematics motion of MAV are expressed in the following equations.

$$184 \begin{bmatrix} \dot{p}_n \\ \dot{p}_e \\ \dot{p}_d \end{bmatrix} = \begin{bmatrix} c\theta c\psi & s\phi s\theta c\psi - c\phi s\psi & c\phi s\theta c\psi + s\phi s\psi \\ c\theta s\psi & s\phi s\theta s\psi + c\phi c\psi & c\phi s\theta s\psi - s\phi c\psi \\ -s\theta & -s\phi c\theta & c\phi c\theta \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} \quad (1)$$

185 where, c stands for cos and s stands for sin respectively in equation 1.

$$186 \begin{bmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix} = \begin{bmatrix} 1 & \sin\phi \tan\theta & \cos\phi \tan\theta \\ 0 & \cos\phi & -\sin\phi \\ 0 & \sin\phi \sec\theta & \cos\phi \sec\theta \end{bmatrix} \begin{bmatrix} p \\ q \\ r \end{bmatrix} \quad (2)$$

187 Let m is the mass of MAV, f_x, f_y, f_z are the component forces acting along the body frame $x,$
188 $y,$ and z axes respectively. Then, the forces and velocities expressed in the body frame of MAV as

$$189 m \left(\frac{dV_g^b}{dt_b} + \omega_{b/i}^b \times V_g^b \right) = f^b \quad (3)$$

190 where, $V_g^b = (u, v, w)^T,$ $\omega_{b/i}^b = (p, q, r)^T,$ $f^b = (f_x, f_y, f_z)^T,$ \times stands for cross product.

191 Equivalently,

$$192 \dot{u} = rv - qw + \frac{f_x}{m} \quad (4)$$

$$194 \dot{v} = pw - ru + \frac{f_y}{m} \quad (5)$$

$$196 \dot{w} = qu - pv + \frac{f_z}{m} \quad (6)$$

The total forces along the body axes are obtained by summing all the components of forces due to

gravity $(f_{x_{gravity}}, f_{y_{gravity}}, f_{z_{gravity}})$, aerodynamics $(f_{x_{aero}}, f_{y_{aero}}, f_{z_{aero}})$ and propulsion $(f_{x_{propulsion}}, f_{y_{propulsion}}, f_{z_{propulsion}})$.

$$f_x = f_{x_{gravity}} + f_{x_{aero}} + f_{x_{propulsion}} \quad (7)$$

$$f_y = f_{y_{gravity}} + f_{y_{aero}} + f_{y_{propulsion}} \quad (8)$$

$$f_z = f_{z_{gravity}} + f_{z_{aero}} + f_{z_{propulsion}} \quad (9)$$

197 Similarly, angular momentum and angular velocities of MAV can be expressed in the body
198 frame as

$$199 \frac{dh^b}{dt_b} + \omega_{b/i}^b \times h^b = m^b \quad (10)$$

200 where, $h^b = J\omega_{b/i}^b$, $m^b = (l, m, n)^T$; l , m , and n are moments acting on the body frame x , y , and z
201 axes respectively and J is inertia matrix.

$$202 J = \begin{bmatrix} J_{xx} & -J_{xy} & -J_{xz} \\ -J_{xy} & J_{yy} & -J_{yz} \\ -J_{xz} & -J_{yz} & J_{zz} \end{bmatrix} \quad (11)$$

203 It is to be noted that in conventional fixed wing vehicles, J_{xy} and J_{yz} are considered as zero;
204 however, in case of ‘‘Skylark’’ MAV, these values are not negligible due to the presence of top wing
205 and asymmetric mass distribution.

206 The propulsive force is calculated based on the available dynamic thrust at a given RPM of the
207 motor. Aerodynamic forces and moments are contributed due to free stream airflow as well as the
208 flow due to the propeller. In the case of MAV, the propeller’s contribution to the aerodynamic force
209 is quite substantial (Sudhakar et al. 2017), and it should be included in the design. The effect of
210 propeller flow on the dynamics is separately modeled considering the only flow of propeller with
211 the variation of motor RPM in zero free stream velocity. The component of forces and moments
212 due to propeller flow is modeled as a function of motor RPM (ω). The ‘‘Skylark’’ MAV has an

213 elevon control surface, and its effect can be modeled as a combination of individual elevator and
 214 aileron control surface. The aerodynamic forces and moments will mainly depend on the the angle
 215 of attack (α), roll rate (p), pitch rate (q), yaw rate (r), elevator angle (δ_e), aileron angle (δ_a) and
 216 flow due to propeller motion.

$$217 \quad f_{\text{Total}}(\alpha, p, q, r, \delta_e, \delta_a, \omega) = f_{\text{Free-stream}}(\alpha, p, q, r, \delta_e, \delta_a) + f_{\text{Propeller-flow}}(\omega) \quad (12)$$

$$218 \quad m_{\text{Total}}(\alpha, p, q, r, \delta_e, \delta_a, \omega) = m_{\text{Free-stream}}(\alpha, p, q, r, \delta_e, \delta_a) + m_{\text{Propeller-flow}}(\omega) \quad (13)$$

220 Lift and drag forces are measured in the stability frame. The main parameters affecting the
 221 lift and drag forces are the angle of attack (α), pitch rate (q), elevator angle (δ_e), and flow due to
 222 propeller motion. Lift force is modeled along with the stability axis frame as follows:

$$223 \quad F_{\text{Lift}} = \frac{1}{2} \rho V_a^2 S C_L(\alpha, q, \delta_e) + f_L(\omega) \quad (14)$$

$$224 \quad F_{\text{Drag}} = \frac{1}{2} \rho V_a^2 S C_D(\alpha, q, \delta_e) + f_D(\omega) \quad (15)$$

225 where C_L and C_D are the lift coefficient and drag coefficient, $f_L(\omega)$ and $f_D(\omega)$ are the contribution
 226 of propeller flow towards the lift and drag forces, ρ is the density of air, V_a is the airspeed, and S is
 227 the reference area of the ‘‘Skylark’’ MAV. C_L and C_D are modeled with acceptable accuracy as

$$228 \quad C_L = C_L(\alpha) + C_{L_q} \frac{c}{2V_a} q + C_L(\delta_e) \quad (16)$$

$$229 \quad C_D = C_D(\alpha) + C_{D_q} \frac{c}{2V_a} q + C_D(\delta_e) \quad (17)$$

231 where, c is the chord of the bottom wing. The aerodynamic forces $f_{x_{\text{aero}}}$ and $f_{z_{\text{aero}}}$ are obtained after
 232 transforming F_{Lift} and F_{Drag} in body frame.

233 Similarly, the aerodynamic lateral force acting along y-axis depend on the sideslip angle (β),
 234 roll rate (p), yaw rate (r), aileron deflection (δ_a) and effect of propeller flow. The lateral force is

235 modeled as follows:

$$236 \quad f_{y_{\text{aero}}} = \frac{1}{2}\rho V_a^2 S C_Y(\beta, p, r, \delta_a) + f_Y(\omega) \quad (18)$$

$$237 \quad C_Y = C_Y(\beta) + C_{Y_p} \frac{b}{2V_a} p + C_{Y_r} \frac{b}{2V_a} r + C_Y(\delta_a) \quad (19)$$

238 where, $f_Y(\omega)$ is the contribution of propeller flow towards lateral force, and b is the span of the
 239 bottom wing. The important factors which contribute to the rolling moment are sideslip angle (β),
 240 roll rate (p), yaw rate (r), aileron deflection (δ_a), flow due to propeller and motor counter-torque.
 241 So, the rolling moment is modeled as:

$$242 \quad l = \frac{1}{2}\rho V_a^2 S b C_l(\beta, p, r, \delta_a) + f_l(\omega) \quad (20)$$

$$243 \quad C_l = C_l(\beta) + C_{l_p} \frac{b}{2V_a} p + C_{l_r} \frac{b}{2V_a} r + C_l(\delta_a) \quad (21)$$

245 where $f_l(\omega)$ is the moment generated due to propeller flow and motor counter-torque. The
 246 moment generated from propeller flow is due to the creation of asymmetric flow around the
 247 propeller. In case of pitching moment, The angle of attack (α), pitch rate (q), elevator deflection
 248 (δ_e), and propeller flow are the main contributing factors. Therefore, pitching moment is modeled
 249 as:

$$250 \quad m = \frac{1}{2}\rho V_a^2 S c C_m(\alpha, q, \delta_e) + f_m(\omega) \quad (22)$$

$$251 \quad C_m = C_m(\alpha) + C_{m_q} \frac{c}{2V_a} q + C_m(\delta_e) \quad (23)$$

253 Similarly, the important variables behind the yawing moment are the same as the rolling moment,
 254 i.e., sideslip angle (β), roll rate (p), yaw rate (r), aileron angle (δ_a), and propeller flow. Yawing
 255 moment is modeled as

$$256 \quad n = \frac{1}{2}\rho V_a^2 S b C_n(\beta, p, r, \delta_a) + f_n(\omega) \quad (24)$$

$$C_n = C_n(\beta) + C_{n_p} \frac{b}{2V_a} p + C_{n_r} \frac{b}{2V_a} r + C_n(\delta_a) \quad (25)$$

The contribution of propeller flow towards various forces and moments are listed in Table 4. The different coefficients of the force and moment equations are obtained through the wind tunnel test and using empirical formulas (Roskam 1990). The estimation method for the different coefficients in force and moment equations are listed in Table 8. The wind tunnel test of “Skylark” is conducted in closed test sections in an open circuit wind tunnel at Micro Air Vehicle Aerodynamic Research Tunnel (MART) in National Aerospace Laboratory (NAL) complex (Jana et al. 2020). The important wind tunnel characteristics are given in Table 5. The snapshot of the MAV placed in the wind tunnel is shown in Figure 5. The wind tunnel test is performed at the velocity range of 6-16 m/s and at different position of angle of attack ($0^\circ - 32^\circ$), angle of sideslip (-7° to 7°), motor RPM (9500-13500 RPM) and control surfaces. The static and control derivatives are listed in Table 6 and Table 7.

The plant’s non-linear model is linearized at the different operating points of the flight envelope for ease of controller design, and the static stability is checked at all points. The plant is linearised at different velocities ranging from 8-12 m/s and different flight conditions such as straight and level flight, climbing flight, turning flight. The non linear model of MAV, $\dot{x} = f(x, u)$ and $y = f(x)$ can be linearised about any operating point as:

$$\dot{x} = Ax + Bu; \quad y = Cx \quad (26)$$

where, x, u, y are the MAV states, control, and output variables; A, B, C are the system matrix, control input matrix, and output matrix.

The important states and control variables which affect the longitudinal dynamics are velocity in forward and downward direction, pitch rate, pitch angle, elevator and throttle input. In the case of straight and level flight at the velocity of 10 m/s, longitudinal dynamics for state variables ($(x_{\text{long}}) = (u, w, q, \theta)^T$) and control variables ($(u_{\text{long}}) = (\delta_e, \delta_t)^T$) can be expressed as:

282

$$\dot{x}_{\text{long}} = A_{\text{long}}x_{\text{long}} + B_{\text{long}}u_{\text{long}}. \quad (27)$$

In this case,

$$A_{\text{long}} = \begin{pmatrix} -1.091 & 0.3773 & -1.832 & -9.641 \\ -0.6549 & -3.944 & 9.714 & -1.796 \\ 38.16 & -56.61 & -1.569 & 0 \\ 0 & 0 & 0.991 & 0 \end{pmatrix}$$

$$B_{\text{long}} = \begin{pmatrix} -0.3478 & 33.54 \\ 2.424 & -17.66 \\ -567.7 & -738.7 \\ 0 & 0 \end{pmatrix}$$

283 Similarly, lateral dynamics mainly depends on lateral velocity, roll rate, yaw rate and roll angle,
 284 and aileron input. The lateral dynamics can be expressed as for state ($x_{\text{lat}} = (v, p, r, \phi)^T$) and
 285 control ($u_{\text{lat}} = (\delta_a, \delta_r)^T$) is expressed as ;

286

$$\dot{x}_{\text{lat}} = A_{\text{lat}}x_{\text{lat}} + B_{\text{lat}}u_{\text{lat}}. \quad (28)$$

287

In this case,

$$A_{\text{lat}} = \begin{pmatrix} -0.8921 & 1.855 & -9.834 & 9.554 \\ -32.38 & -0.1321 & 0.1738 & 0 \\ 11.91 & -0.0335 & -3.326 & 0 \\ 0 & 1.0 & 0.1862 & 0 \end{pmatrix}$$

$$B_{\text{lat}} = \begin{pmatrix} 1.764 & 2.102 \\ 132.0 & -116.7 \\ 109.2 & -58.29 \\ 0 & 0 \end{pmatrix}$$

288 The different modes of the MAV are shown in Table 9. In the case of longitudinal dynamics, the
 289 complex pairs $(-2.4476 + 24.8028i$ and $-2.4476 - 24.8028i)$ are related to short period modes, and
 290 other pairs $(-0.8544 + 1.4212i$ and $-0.8544 - 1.4212i)$ are responsible for phugoid modes. Similarly,
 291 in the case of lateral dynamics, the complex pairs $(-0.7032 + 13.0454i$ and $-0.7032 - 13.0454i)$ are
 292 related to dutch-roll mode; however, in this case, the rolling mode and the spiral mode cannot be
 293 distinguished as typically done in larger UAVs.

294 Clearly, from Table 9, the longitudinal and lateral dynamics are statically stable for this operating
 295 point. Similarly, the static stability of different operating points at different flight conditions is
 296 checked and found to be stable. In the case of MAV, the coupled lateral and longitudinal model can
 297 be unstable, although the separate dynamics can be stable (Harikumar et al. 2016). In this case, the
 298 coupled dynamics for state $(x_{\text{coupled}} = (u, w, q, \theta, v, p, r, \phi)^T)$ and control $(u_{\text{coupled}} = (\delta_e, \delta_a, \delta_t)^T)$
 299 is expressed as ,

$$300 \quad \dot{x}_{\text{coupled}} = A_{\text{coupled}}x_{\text{coupled}} + B_{\text{coupled}}u_{\text{coupled}} \quad (29)$$

301 The system matrix A_{coupled} is given by:

$$302 \quad A_{\text{coupled}} = \begin{pmatrix} -1.091 & 0.3773 & -1.832 & -9.641 & 0.0269 & 0 & -0.07 & 0 \\ -0.65 & -3.94 & 9.71 & -1.796 & 0.01 & 0.07 & 0 & 1.29 \\ 38.16 & -56.61 & -1.569 & 0 & -0.3467 & -0.002 & -0.0516 & 0 \\ 0 & 0 & 0.991 & 0 & 0 & 0 & 0.134 & -0.0197 \\ 0.20 & 0.038 & 0 & 0.2428 & -0.8921 & 1.855 & -9.834 & 9.554 \\ 4.07 & -0.1638 & -0.027 & 0 & -32.38 & -0.1321 & 0.1738 & 0 \\ 2.429 & -0.90 & -0.04 & 0 & 11.91 & -0.0335 & -3.326 & 0 \\ 0 & -0.02 & 0 & 0 & 0 & 1.0 & 0.1862 & 0 \end{pmatrix}$$

303 The different modes of this coupled dynamics are shown in Table 10. Comparing the eigenvalues
 304 of separate dynamics (from Table 9) with the coupled dynamics (from Table 10), it is observed that

305 the eigenvalues are close to each other. It can be concluded that the effect of coupling is small for
306 this MAV configuration; hence, the controller design for the longitudinal dynamics and the lateral
307 dynamics can be performed separately.

308 **ALGORITHM DESIGN**

309 In this section, important algorithms required for an autonomous mission such as estimation,
310 controller, and path planning algorithms are discussed. Accurate state estimation is of utmost
311 importance for the system identification using the flight tests, guidance, and controller design of
312 MAV. The overall mission is classified into different waypoints. The waypoint information is passed
313 through the guidance block, and the desired height and course angle information are generated.
314 For ease of implementation of guidance block, the guidance commands for the controller block
315 can be generated using Lyapunov based vector field method (Nelson et al. 2007), (Lawrence et al.
316 2008), nonlinear guidance motivated from proportional navigation guidance algorithm (Park et al.
317 2004). In overall system architecture, the controller block must be designed very much specific
318 to the vehicle dynamics. In an ideal case, the controller should be designed at different operating
319 points, and gains are selected using gain scheduling techniques. The different operating points are
320 mainly decided based on the airspeed, angle of attack, height. In this case, the airspeed and the
321 angle of attack information are not available accurately; hence it is difficult to schedule the gains
322 based on the operating points. So, the controller is designed considering the best representative
323 plant. The controller is designed for a straight and level flight for the nominal velocity of 10 m/s.
324 As discussed earlier, the coupling effects of longitudinal and lateral dynamics are not significant;
325 hence, the controller for longitudinal dynamics and lateral dynamics is designed separately.

326 **Controller Design**

327 The controller block generates the control commands for the motor and control servos after
328 considering the desired commands from the guidance loop and the MAV's present state from the
329 estimation loop. Apart from ensuring overall system stability, controller design must be performed
330 considering the handling qualities that determine the aircraft responses to external disturbances
331 or pilot commands. In the MAV class of vehicles, no specification for the handling qualities

332 requirement is available in the open literature. So, the specifications for controller design are
 333 considered from the MIL-F8785C with suitable adjustment for the MAV class of vehicles. The
 334 "Skylark" is classified as Class-IV and the controller design specifications are obtained considering
 335 flight operation in the category of phase C with a level of acceptability to be one. With this
 336 consideration, the controller design specifications from the handling point of view as per MIL-
 337 F8785C is shown in Table 11, ω_{n_s} , ω_{n_d} , ζ_s , ζ_{ph} , ζ_d are the short period frequency, dutch roll mode
 338 frequency, short period damping ratio, and phugoid mode damping ratio respectively (Sadraey
 339 2012). Comparing the desired value and the present value of different parameters in Table 11, it
 340 is concluded that ζ_s and ζ_d , i.e., damping of the short period and the dutch roll mode needs to be
 341 improved.

342 The controller structure needs to be chosen to improve the damping of short period mode and
 343 dutch roll mode. The short period mode is motion in pitch plane involving pitch rate (q), pitch
 344 attitude (θ), and angle of attack (α). The dutch roll is an oscillation in the yaw plane, which
 345 combines roll and sideslip.

346 In the case of lateral dynamics, the transfer function from $p(s)$ to $\delta_a(s)$:

$$347 \frac{p(s)}{\delta_a(s)} = \frac{131.9s^3 + 518.4s^2 + 50460s - 9090}{s^4 + 4.35s^3 + 180.7s^2 + 510.7s + 1004} \quad (30)$$

351 In the case of longitudinal dynamics, the transfer functions from $q(s)$ to $\delta_e(s)$:

$$352 \frac{q(s)}{\delta_e(s)} = \frac{-566.7s^3 - 3009s^2 - 2764s - 2.159 \times 10^{-14}}{s^4 + 6.604s^3 + 632.3s^2 + 1075s + 1708} \quad (31)$$

353 After closed loop stability analysis, the pitch rate feedback is given to the elevator to improve
 354 the damping of short period mode. Similarly, roll rate feedback is given to the aileron to improve
 355 the damping of dutch roll mode. The lateral and the longitudinal controller block is driven by
 356 the desired course angle (χ_c) and the desired height (h_c) generated from the guidance block,

357 respectively. The lateral and longitudinal controller block diagram details are shown in Figure 6
358 and Figure 7. In the block diagram, the value of the gain used in the controller structure is presented
359 in Table 12. The closed-loop poles of the lateral and longitudinal dynamics are presented in Table
360 13.

361 **Attitude Estimation**

362 Angular rates (p, q, r) and positions (p_n, p_e, p_d) of MAV are available from the gyroscope and
363 GPS respectively. So, in this case, accurate estimation of attitudes (ϕ, θ, ψ) from the available
364 sensors is most important. Attitude estimation is performed using the Kalman filter framework
365 where the attitude states are propagated using the data from gyroscopes, and the prediction is
366 corrected using the information from the accelerometer and magnetometer. Accelerometer and
367 magnetometer data is susceptible to noise due to vibration and the motor's magnetic flux with
368 motor RPM variation. Multisensor fusion framework is used as data from the accelerometer and
369 the magnetometer is not reliable at all operating points. Attitude estimation block diagram is shown
370 in Fig. 8.

371 The sensor noises variance is calculated to form the sensor data log by conducting the remotely
372 controlled flight tests. The accuracy of the estimation is checked using the motion simulator. In
373 a motion simulator, the rate table is subjected to accurate angular rates, and its accurate angular
374 position is recorded. The inner axis, middle axis, outer axis are subjected to roll, pitch, and yaw
375 rates, respectively. The MAV is fitted with the motion simulator, and the estimation algorithm is
376 verified by comparing the output of the estimator with the motion simulator's actual data. Also,
377 the estimation output is checked after subjecting the vehicle to external vibrations. The estimation
378 algorithm can be checked only with autopilot placement; however, the vehicle itself is put in the
379 simulator just before flight tests to avoid the misalignment and orientation error involved with the
380 placement of autopilot. A typical image during the estimation algorithm testing using motion
381 simulator is shown in Fig. 9.

382 **SIMULATION**

383 The nonlinear MAV model of “SKYLARK” is simulated in MATLAB software. MAV needs to
384 follow the waypoint path. As wind velocity is comparable to MAV velocity, MAVs are susceptible
385 to gust. Total wind vector is considered as a combination of steady-state wind and a stochastic
386 component consists of wind gust and atmospheric disturbances (Beard and McLain 2009). The
387 stochastic gusts components are generated after passing the white noise through the Dryden transfer
388 functions. The 3D coordinates of the waypoints to be followed are shown in Table 14. The guidance
389 commands for the controller block is generated using the vector field method (Nelson et al. 2007).

390 The path followed by the MAV against the desired path is shown in Fig. 10. The tracking of
391 desired course angle, roll angle, roll rate are shown in Fig. 11, Fig. 12, Fig. 13 respectively. The
392 corresponding control command given to the aileron is shown in Fig.14. Similarly, in the case of
393 longitudinal dynamics, Fig. 15, Fig. 16, Fig. 17, and Fig. 18 show the tracking of the desired
394 height, pitch angle, roll rate and the corresponding control input respectively. Clearly, the plant is
395 able to track the desired attitude and attitude rates during the waypoint mission. The control input
396 to elevator (Fig. 18) and aileron (Fig. 14) is also bounded during the mission.

397 **AUTONOMOUS FLIGHT TEST**

398 In this section, details of the autonomous flight test of MAV is discussed. The tentative autopilot
399 software architecture of “Skylark” MAV is shown in Fig. 19. The software architecture used in
400 the autopilot is based on ardupilot firmware. The various sensor information is captured using the
401 sensor acquisition block, and this information is used in the estimation block for state estimation.
402 The estimation frequency is kept higher than the controller frequency. The guidance block generates
403 the desired roll and pitch angle for the controller block. The controller block is operated at 50 Hz.
404 The autopilot software is initially tested through Software in Loop Simulations (SILS) with virtual
405 sensors and inside a virtual environment. The software is then further tested with Hardware in
406 Loop Simulations (HILS) using the real autopilot hardware. HILS is performed with the help of a
407 motion simulator.

408 **Flight Testing**

409 Once the SILS and HILS are performed successfully, the autonomous flight test is carried out
410 in an outdoor environment. Since there are huge uncertainties involved with the manufacturing of
411 MAV, few small duration remote-controlled (RC) flight tests are always performed to adjust the trim
412 values of the control surface deflection before autonomous flights. MAV may undergo intermittent
413 crash landing in this flight stage. After the successful initial RC tests of the vehicle, the system
414 is further cross-checked for autonomous flight tests. The MAV is placed on flat ground, and the
415 attitude angles are checked approximately. If there is an anomaly in the attitude angles, it is fixed
416 after recalibration of the accelerometer and magnetometer as per the standard procedure.

417 MAV is launched with the hand in stabilized mode (Human Pilot is in the loop with autopilot)
418 at an approximately fixed amount of jerk and at a fixed angle of attack. The allowable roll angle
419 for the initial few seconds after launch is fixed to a particular angle. The MAV is subjected to
420 autonomous mode (fully autonomous) once it gained a certain height and a certain velocity. During
421 the take-off stage and landing, it is better to keep the pilot in the loop to counteract sudden gust as
422 MAV is more susceptible to gust at these two critical stages. However, landing can be performed
423 in autonomous mode. Flight test videos are included in this link ¹.

424 **Flight Test Results**

425 "Skylark" has performed several successful flight tests in different weather conditions. One of
426 the successful flight tests is described here. The results of one of several successful autonomous
427 flight tests are described here. In this case, the take-off and landing are performed in a stabilized
428 mode, and in between vehicle is flown in autonomous mode. The MAV is launched from the home
429 location, and the consecutive waypoints are points 1, 2, and 3, respectively. If the MAV has reached
430 within a radius of 30 m of a waypoint, it is considered that vehicle has reached the waypoint. The
431 path of the vehicle using the logged GPS data during the waypoint mission is shown in Fig. 20.
432 Clearly, the vehicle is able to perform the waypoint mission successfully, as it has reached within a
433 radius of 30 m (drawn around the point). The 3D path of the vehicle using the GPS coordinates is

¹Flight test videos

434 shown in Fig. 21. The MAV is launched at point A, and initially, it is in stabilized mode. At point
435 B, the autonomous mode is switched on, and it performed the waypoint mission. After completing
436 the waypoint mission, the MAV is put into stabilized mode again and landed successfully at point
437 D.

438 The tracking response of the vehicle is analyzed from the recorded flight data. The commanded
439 attitude angles and actual attitudes are plotted in Fig. 22, Fig. 24, Fig. 26; where the commanded
440 portion is the duration where the vehicle was flying in autonomous mode. The commanded roll
441 angle from the guidance loop and the achieved roll angle by MAV is shown in Fig. 22. The
442 corresponding roll rate is plotted in Fig. 23. Similarly, the commanded pitch angle, achieved pitch
443 angle, and the corresponding pitch rate is shown in Fig. 24 and Fig. 25. Likewise, for commanded
444 yaw angle, achieved yaw angle, and the corresponding yaw rate is shown in Fig. 26 and Fig. 27.

445 It can be concluded that the tracking responses of the commanded roll and yaw angle are
446 acceptable; however, tracking of pitch angle needs to be improved for improving the performance
447 during the waypoint mission.

448 **DISCUSSIONS**

449 The crucial challenges of the autonomous mission of MAV are addressed through compact
450 system design and efficient algorithm design. In the case of MAV, component placement plays
451 a vital role in managing the CG location and balancing the counter torque. The designed MAV
452 can handle wind speed up to 3 m/s. The tracking performance can vary based on the location of
453 the waypoints and the direction of the wind. MAV can track the waypoints; however, the tracking
454 performance in the longitudinal plane can be improved. Waypoints can be tracked with accuracy
455 up to 20-30 m. The path between one point to another point may not be smooth due to uncertainty
456 in system dynamics and the presence of wind gust. The performance can be improved by reducing
457 the uncertainty in the system dynamics and plant modeling. Due to the complex dynamics involved
458 with the MAV system, there may be uncertainty in MAV modeling. So, in some cases, some of
459 the algorithm's parameters may need to be modified after observation of the flight tests as the
460 developed plant model may not capture the real flight dynamics. It is not easy for a fixed gain

461 based controller to handle the uncertainties involved in the complex MAV dynamics. An advanced
462 controller, such as an adaptive controller, needs to be considered for the MAV controller design to
463 adapt to uncertain MAV dynamics.

464 **CONCLUSIONS**

465 In this paper, autonomous navigation of a fixed-wing nonconventional biplane MAV “Skylark”,
466 having span and chord length within 150 mm, is presented. The main challenges of an autonomous
467 mission for overall system integration, model development, and controller design are addressed.
468 The key issues of overall vehicle configuration design, such as weight budget, power budget,
469 CG management, balancing counter-torque, are addressed through proper selection, design, and
470 strategical placement of avionics components. The significant effects of motor counter torque and
471 propeller flow on the MAV dynamics are considered to develop a detailed mathematical model
472 through wind tunnel tests. The controller is designed after a detailed analysis of the mathematical
473 model and validated through six-dof simulation, SILS and HILS. Finally, the autonomous flight
474 test is performed successfully through multiple waypoints. It is recommended that the uncertainties
475 involved in the system dynamics need to be handled properly for better mission performance. The
476 proposed design approach for autonomous navigation in this paper will improve the capabilities of
477 the MAV class of vehicles.

478 **DATA AVAILABILITY STATEMENT**

479 Some or all data, models, or code that support the findings of this study are available from the
480 corresponding author upon reasonable request.

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599

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TABLE 1. Important MAV parameters

Parameters	Value
Designed take-off mass	110 g
Nominal velocity	10 m/s
Top wing span	150 mm
Top wing chord	85 mm
Bottom wing span	150 mm
Bottom wing chord	140 mm
Vertical tail (area)	5600 mm ²
Vertical tail (height)	80 mm
Top wing airfoil	Modified MH-60
Bottom wing airfoil	Modified MH-60
Control surface	Elevon
Motor	AP05 5000 kv
Propeller	GWS 5030

TABLE 2. MAV avionics

Component	Description
Main controller unit	i.MX6 Freescale dualcore processor
Sensors	IMU (MPU-9250)
	Altimeter(MS5803-01BA)
	GPS (ORG-1411)
Telemetry	camera
ESC	DRF4463F(433 MHz)
Battery	YEP-7A
	2S: 300 mAh 35-70 C
RAM	1S: 270 mAh 15 C
	512 MB

TABLE 3. MAV moment of inertia

Axis	Value
J_{xx}	$3.3211 \times 10^{-4} \text{ kg} - \text{m}^2$
J_{yy}	$2.7542 \times 10^{-4} \text{ kg} - \text{m}^2$
J_{zz}	$3.0309 \times 10^{-4} \text{ kg} - \text{m}^2$
J_{xy}	$0.0323 \times 10^{-4} \text{ kg} - \text{m}^2$
J_{xz}	$0.7618 \times 10^{-4} \text{ kg} - \text{m}^2$
J_{yz}	$0.0536 \times 10^{-4} \text{ kg} - \text{m}^2$

TABLE 4. Propeller contribution at zero free-stream velocity

Quantity	Value
$f_L(\omega)$	$0.0022 - 4.6\delta_\omega + 11\delta_\omega^2 - 5.8\delta_\omega^3$
$f_D(\omega)$	$-0.003466 + 15.86\delta_\omega - 52.19\delta_\omega^2 + 57.52\delta_\omega^3 - 21.01\delta_\omega^4$
$f_Y(\omega)$	$6.658 \times 10^{-7} - 0.4782\delta_\omega + 1.188\delta_\omega^2 - 0.639\delta_\omega^3$
$f_l(\omega)$	$0.00041 + 0.05326\delta_\omega - 0.1351\delta_\omega^2 + 0.06991\delta_\omega^3$
$f_m(\omega)$	$-0.00019 + 0.33\delta_\omega - 0.8229\delta_\omega^2 + 0.4173\delta_\omega^3$
$f_n(\omega)$	$-0.0000997 + 0.01316\delta_\omega - 0.03349\delta_\omega^2 + 0.01925\delta_\omega^3$

TABLE 5. Wind tunnel details

Specification	Value
Contraction ratio	9:1
Test section	0.8 m x 1.2 m x 2.5m
Velocity range	1-45 m/s
Mean flow velocity variation	+/- 0.1 percent
Flow angularity	< 0.1 ⁰
Free stream turbulent intensity	<0.18 percent
Range of angle of attack	-5 ⁰ – 32 ⁰
Range of sideslip angle	-7 ⁰ – +7 ⁰

TABLE 6. Static and control derivatives

Derivatives	Value at free-stream velocity of 8 m/s
$C_L(\alpha)$	$-0.065 + 2.9\alpha - 2\alpha^2$
$C_L(\delta_e)$	$0.92 \delta_e$
$C_D(\alpha)$	$0.15 + 0.1\alpha + 1.5\alpha^2$
$C_D(\delta_e)$	$-0.06332\delta_e + 0.176\delta_e^2$
$C_Y(\beta)$	$0.05 - 0.58\beta$
$C_Y(\delta_a)$	$0.1148\delta_a$
$C_l(\beta)$	$-0.46\beta - 0.0059$
$C_l(\delta_a)$	$0.14\delta_a$
$C_m(\alpha)$	$0.24 - 0.73\alpha,$
$C_m(\delta_e)$	$-0.5617\delta_e + 0.5703\delta_e^2$
$C_n(\beta)$	$0.24\beta - 0.011$
$C_n(\delta_a)$	$0.09087\delta_a$

TABLE 7. Dynamic derivatives

Derivatives	Value
C_{L_q}	1.1339,
C_{D_q}	0
C_{Y_p}	0.0
C_{Y_r}	0.0
C_{l_p}	-0.0216
C_{l_r}	0.1639
$C_m(q)$	-0.2609
C_{n_p}	0.0
C_{n_r}	-0.5375

TABLE 8. Model parameter estimation

Quantity	Wind tunnel test	Empirical formula
Lift force	$C_L(\alpha), C_L(\delta_e), f_L(\omega)$	C_{Lq}
Drag force	$C_D(\alpha), C_D(\delta_e), f_D(\omega)$	C_{Dq}
Side force	$C_Y(\beta), C_Y(\delta_a), f_Y(\omega)$	C_{Yp}, C_{Yr}
Rolling moment	$C_l(\beta), C_l(\delta_a), f_l(\omega)$	C_{lp}, C_{lr}
Pitching moment	$C_m(\alpha), C_m(\delta_e), f_m(\omega)$	C_{mq}
Yawing moment	$C_n(\beta), C_n(\delta_a), f_n(\omega)$	C_{np}, C_{nr}

TABLE 9. Different modes of MAV

Longitudinal dynamics	Lateral dynamics
-2.4476 +24.8028i	-0.7032 +13.0454i
-2.4476 -24.8028i	-0.7032 -13.0454i
-0.8544 + 1.4212i	-1.4718 + 1.9285i
-0.8544 - 1.4212i	-1.4718 - 1.9285i

TABLE 10. Different modes of coupled dynamics of MAV

Coupled dynamics	Coupled dynamics
$-2.4484 + 24.8023i$	$-0.70 + 13.0556i$
$-2.4484 - 24.80323i$	$-0.70 - 13.0556i$
$-0.9266 + 1.3067i$	$-1.4020 + 1.9750 i$
$-0.9266 + 1.3067i$	$-1.4020 - 1.9750 i$

TABLE 11. Handling qualities requirement as per MIL-F8785C

Parameters	Desired value	Present value
ω_{n_s}	0.4 (minimum)	24.92 rad/s
ω_{n_d}	1.0 (minimum)	13.064 rad/s
ζ_s	0.35-1.3	0.098
ζ_{ph}	0.04 (minimum)	0.515
ζ_d	0.08 (minimum)	0.05
$\zeta_d \omega_{n_d}$	1	0.65

TABLE 12. Different parameters of controller structure

Lateral dynamics		Longitudinal dynamics	
Gain variable	Value	Gain variable	Value
$k_{i\chi}$	2.56	k_{ih}	1.41
$k_{p\chi}$	2.86	k_{ph}	1.36
$k_{p\phi}$	0.021	$k_{i\theta}$	-0.001
$k_{p\phi}$	0.4	$k_{p\theta}$	-4.5
k_{ip}	-0.018	k_{pq}	-0.15
k_{pp}	0.002		

TABLE 13. Closed loop poles of MAV

Longitudinal dynamics	Lateral dynamics
-77.9484 +0.0i	-0.589 +13.21i
-12.2718 +0.0i	-0.589 -13.21i
-0.6944 + 1.1416i	-0.0238 + 0.525i
-0.6944 - 1.1416i	-0.0238 - 0.525i

TABLE 14. Waypoint path following

Points	Co-ordinates
Initial position	(0,0,0)
Point 1	(50,0,20)
Point 2	(400, 0, 20)
Point 3	(200,200, 20)
Point 4	(0,0, 10)

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641 27 Yaw rate 70

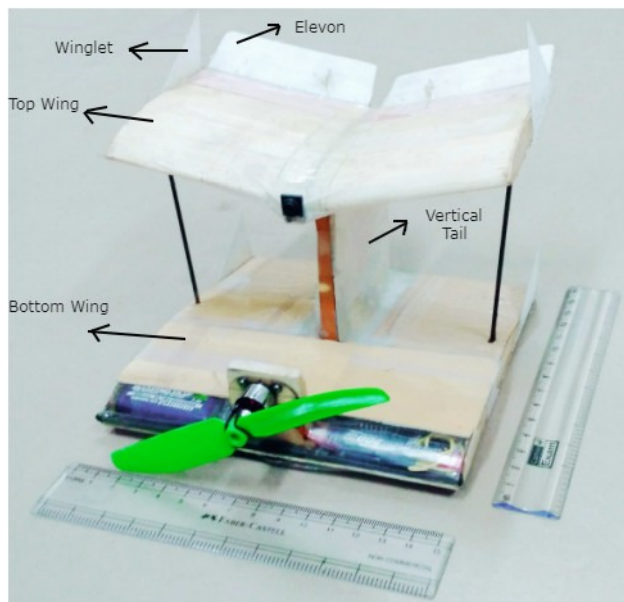


Fig. 1. "Skylark" MAV

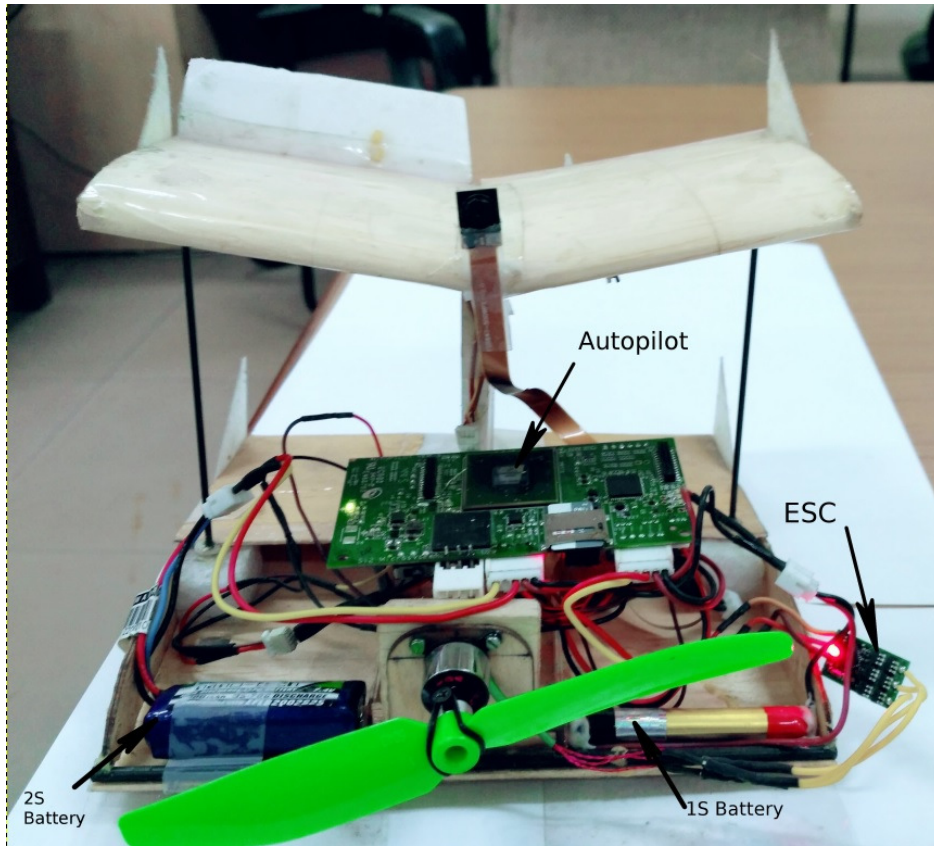


Fig. 2. MAV avionics

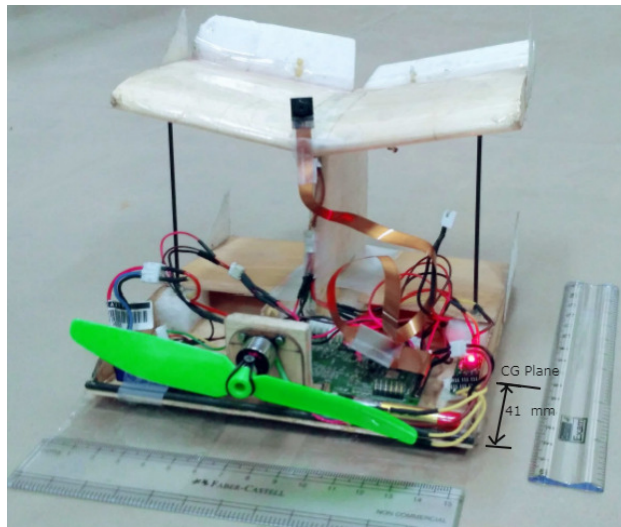


Fig. 3. Component placement

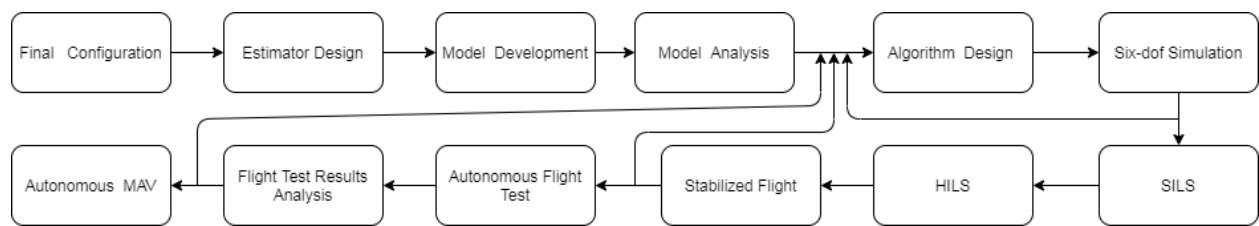


Fig. 4. Autonomous navigation flow chart

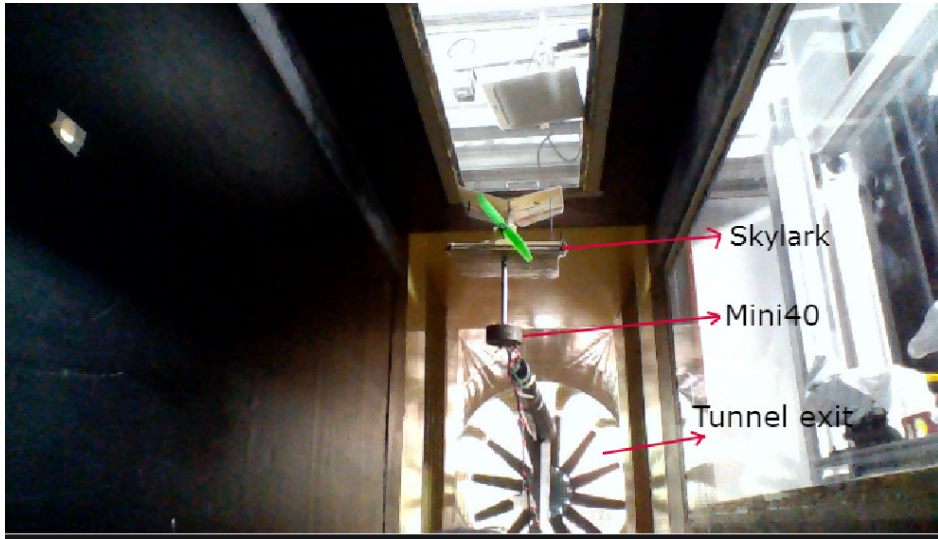


Fig. 5. Snapshot of MAV placed in windtunnel

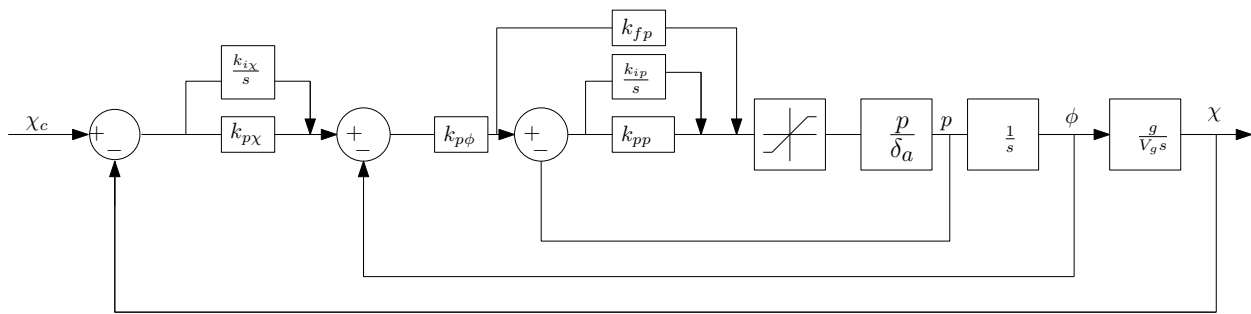


Fig. 6. Lateral controller structure

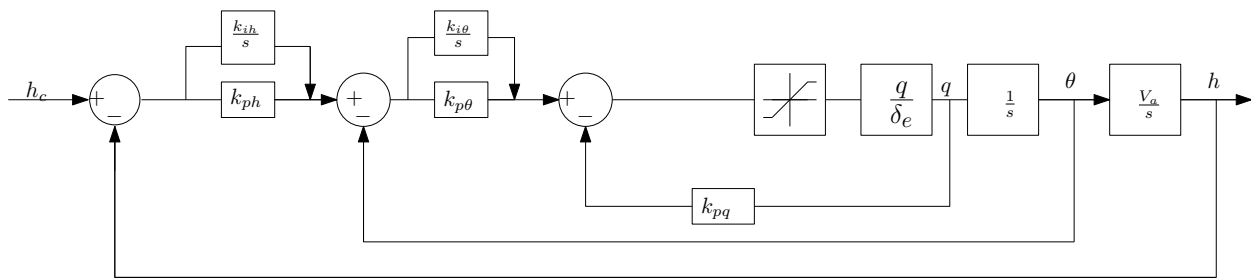


Fig. 7. Longitudinal controller structure

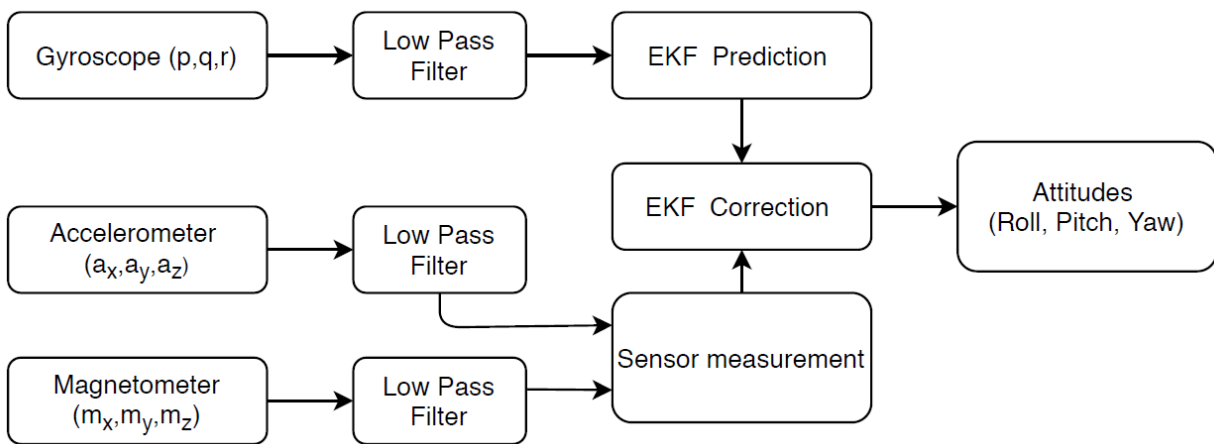


Fig. 8. Estimation block



Fig. 9. Motion simulator

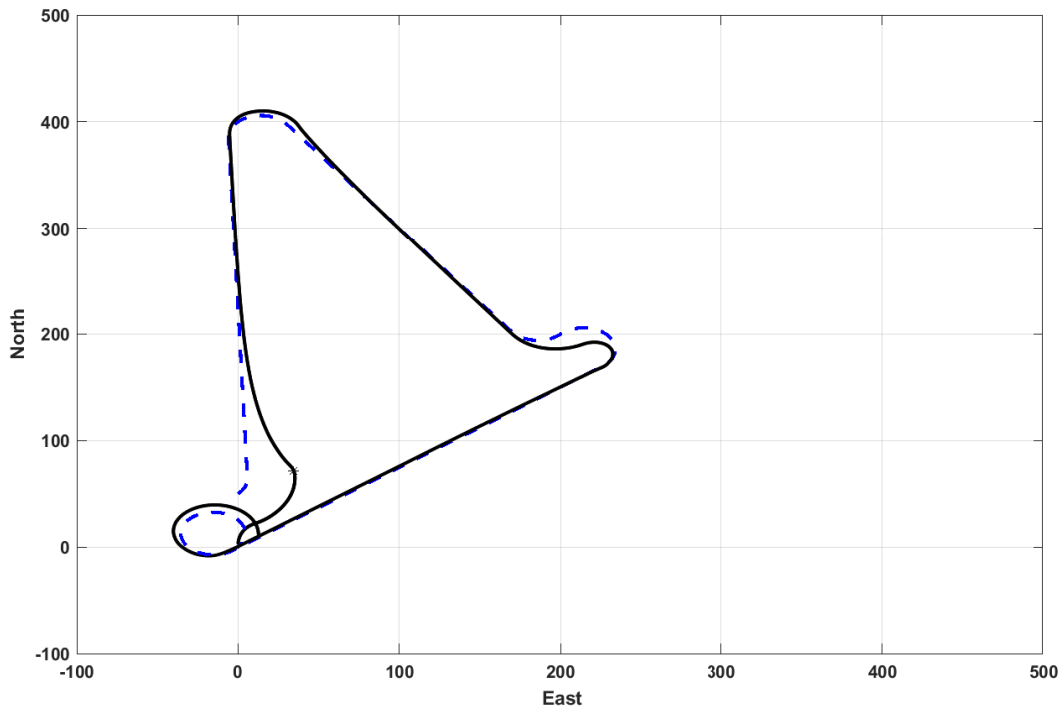


Fig. 10. Waypoint following (simulation): Solid line-Actual path, Dashed line-Desired path

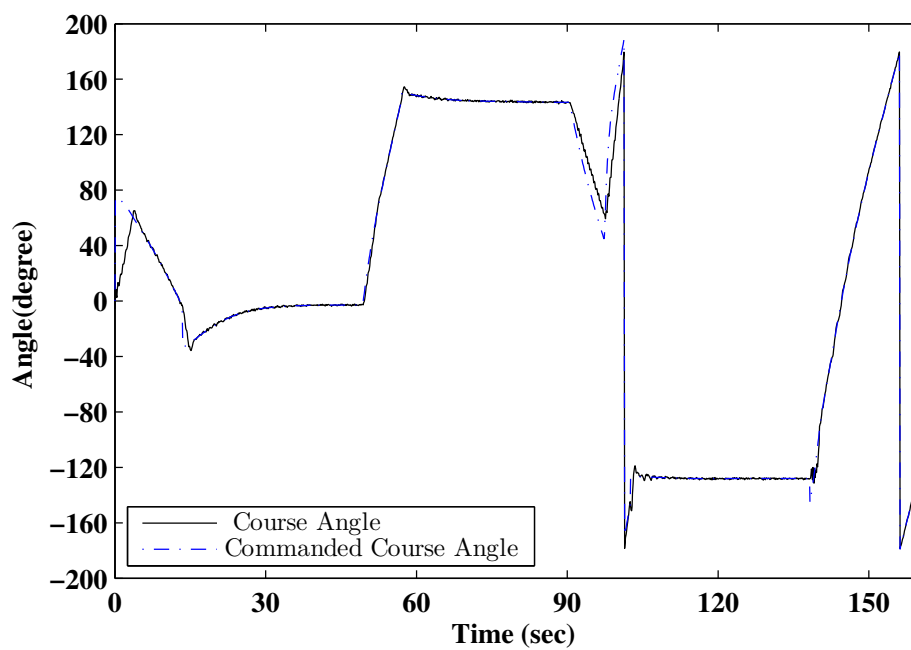


Fig. 11. Tracking of desired course angle

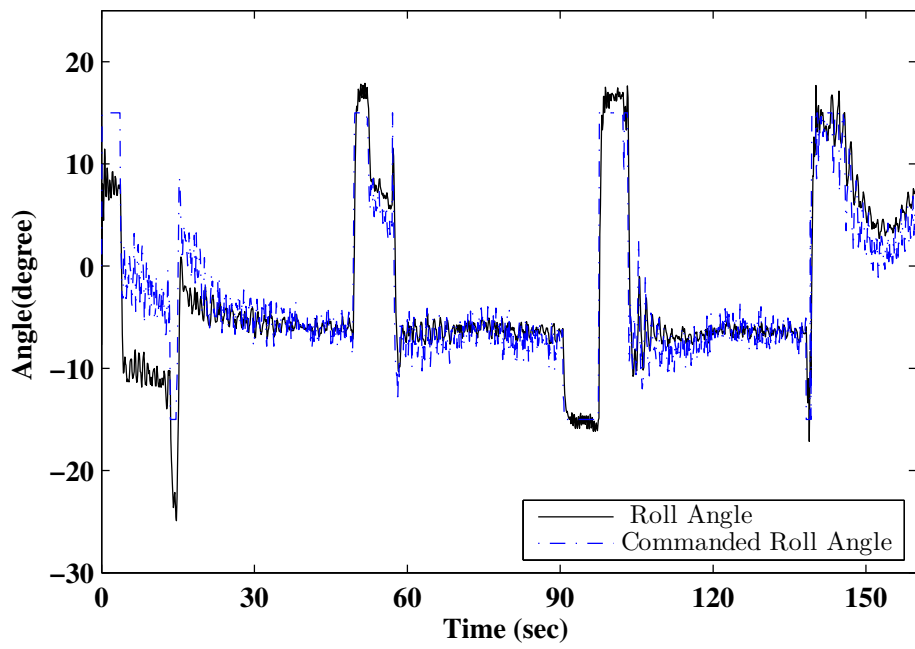


Fig. 12. Tracking of desired roll angle

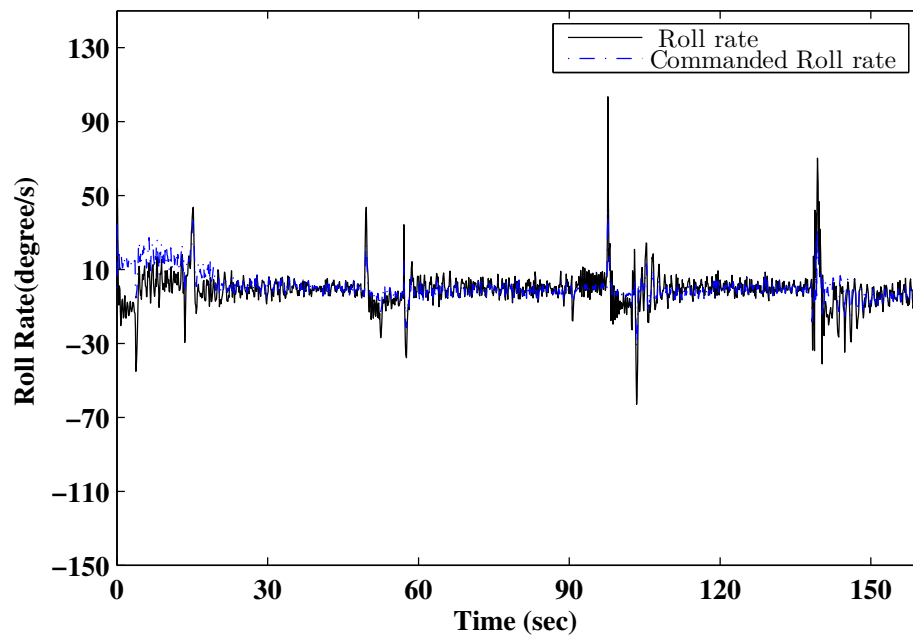


Fig. 13. Tracking of desired roll rate

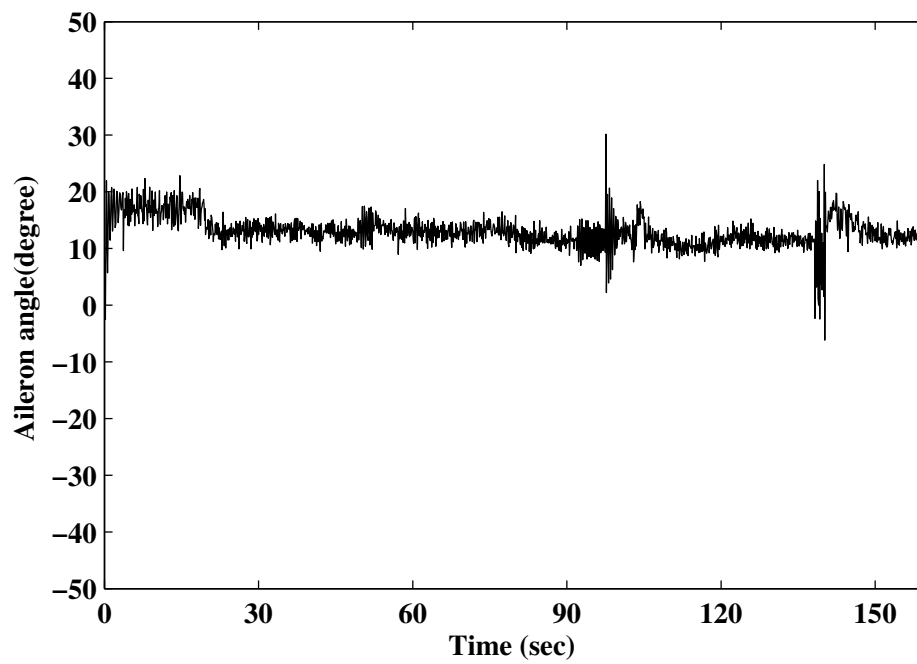


Fig. 14. Aileron Command

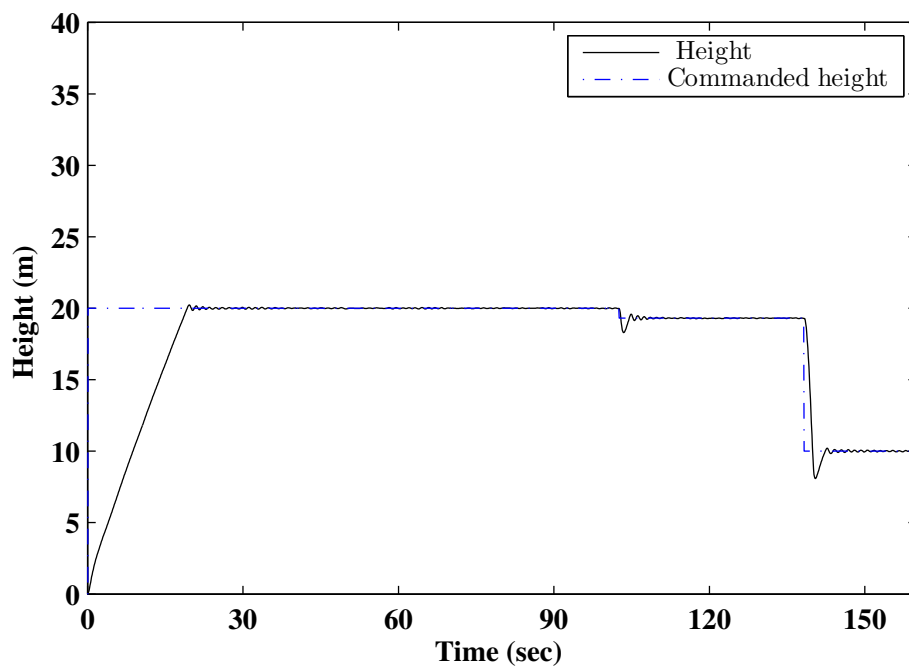


Fig. 15. Tracking of desired height

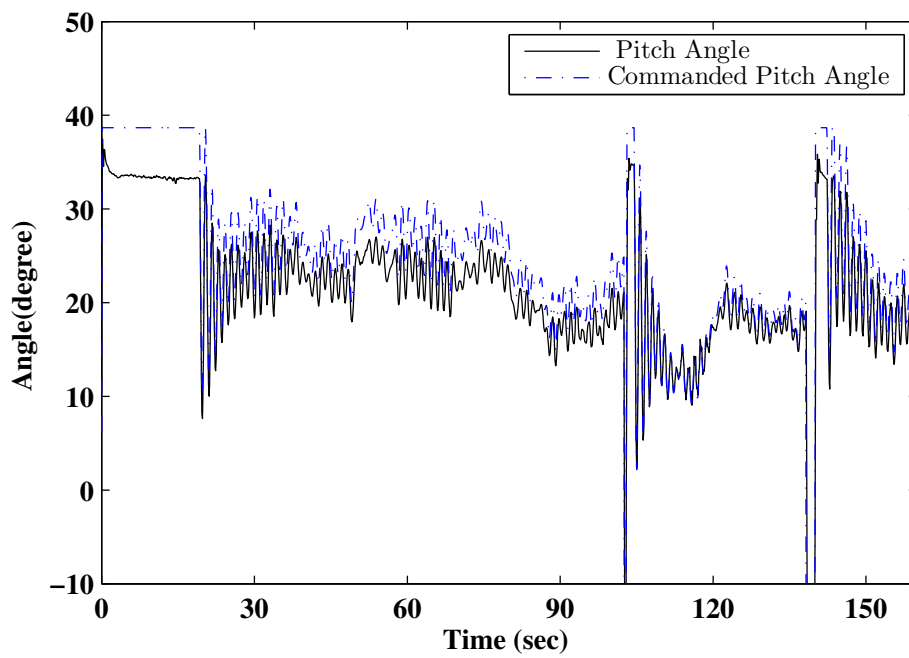


Fig. 16. Tracking of desired pitch angle

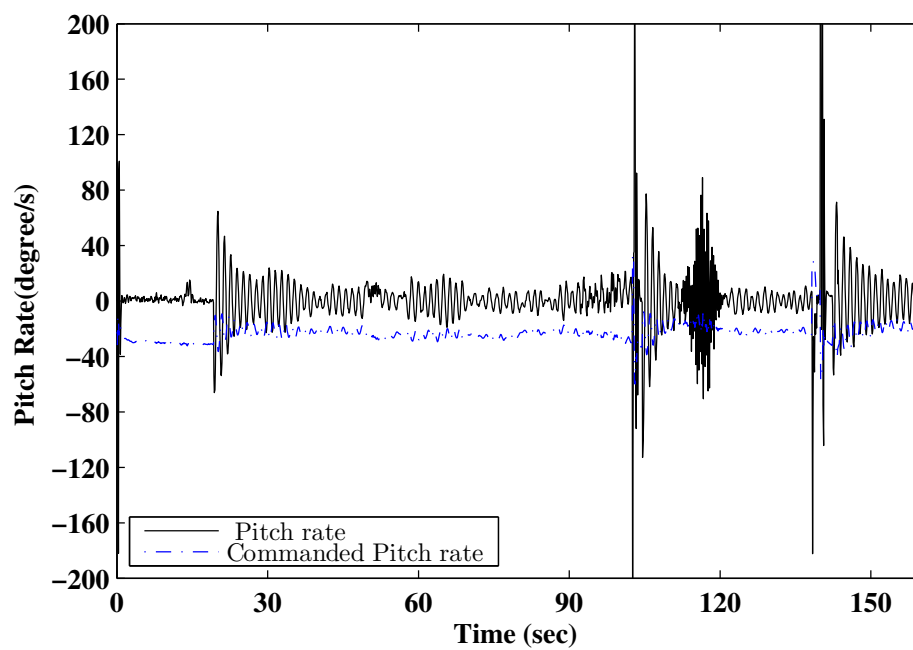


Fig. 17. Tracking of desired pitch rate

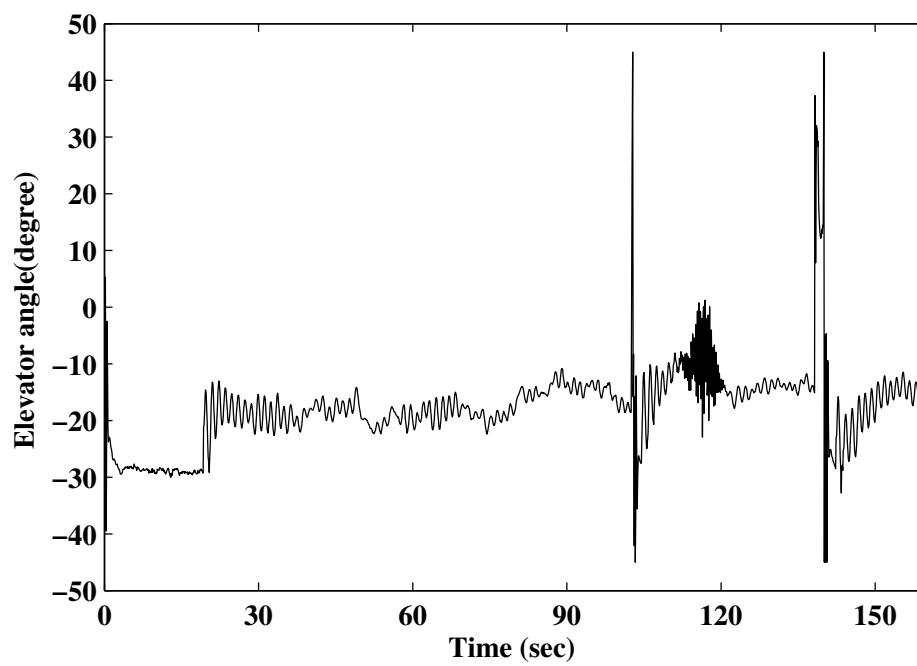


Fig. 18. Elevator Command

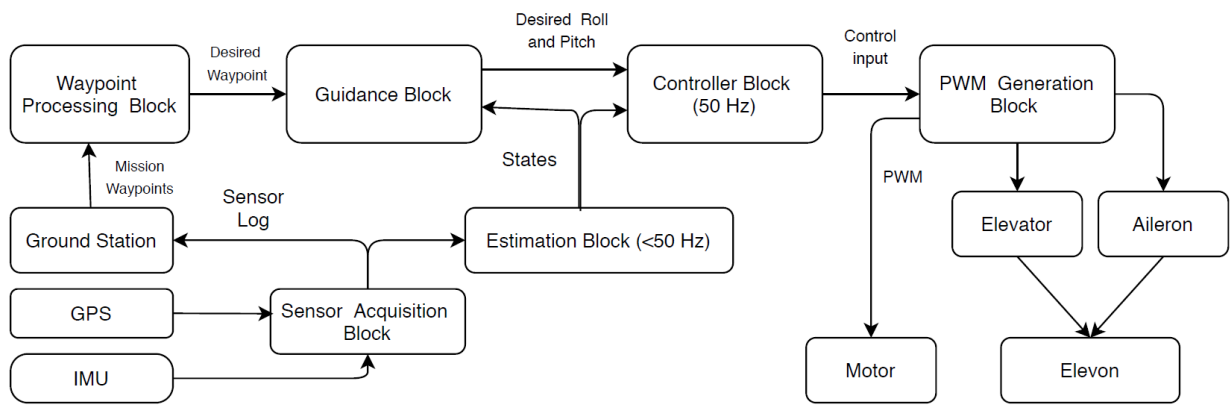


Fig. 19. Flow diagram for waypoint mission implementation

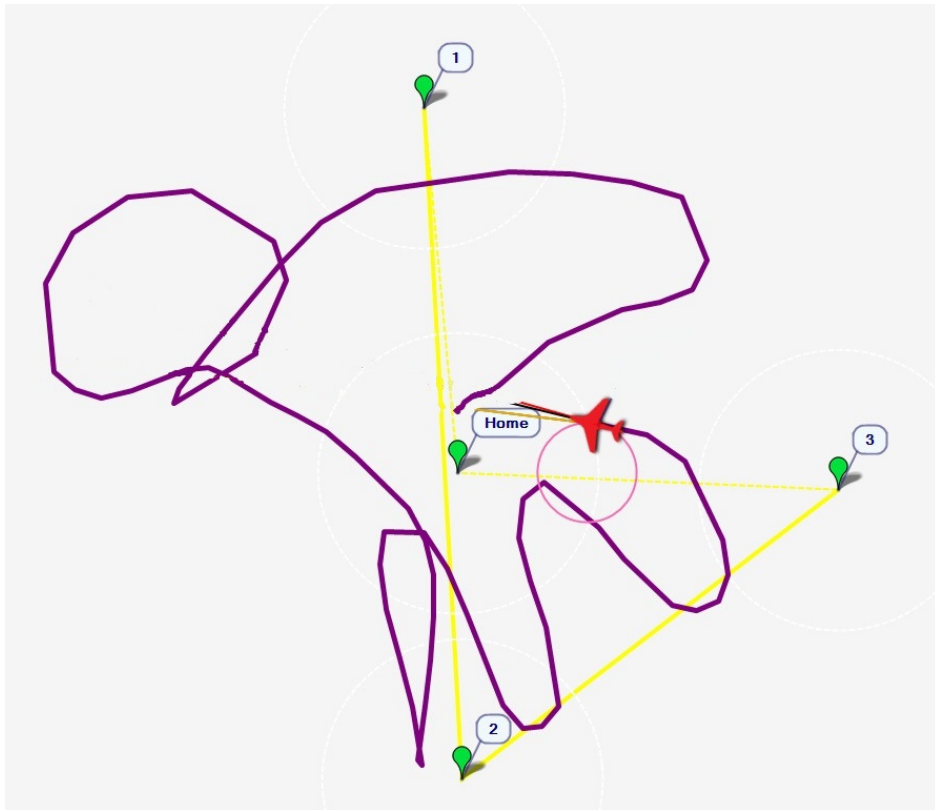


Fig. 20. Tracking of waypoint

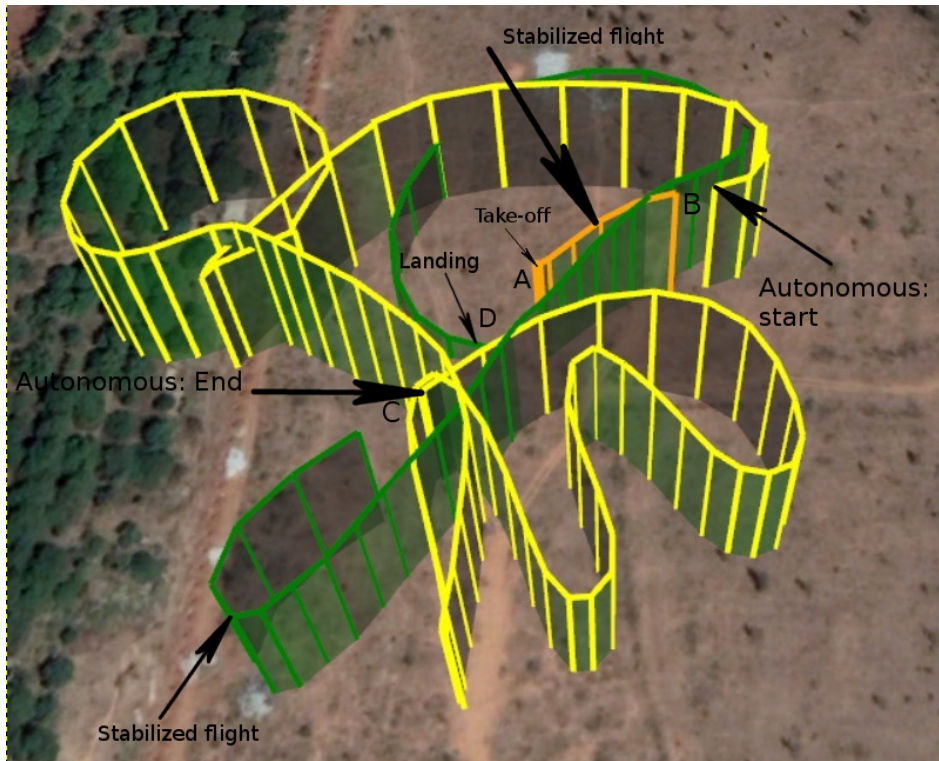


Fig. 21. 3D path during waypoint following

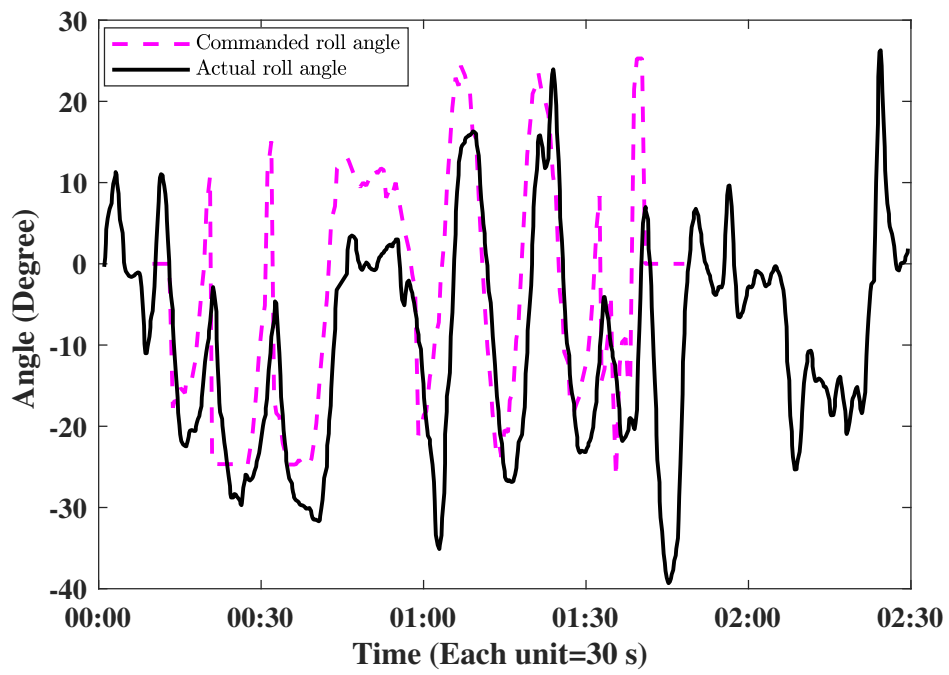


Fig. 22. Commanded roll angle vs Actual roll angle

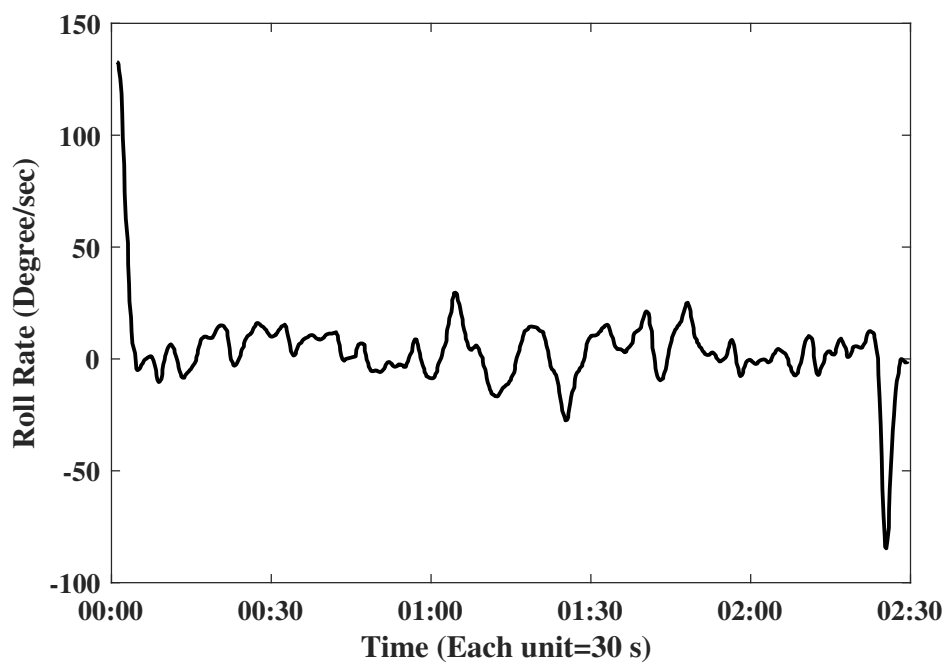


Fig. 23. Roll rate

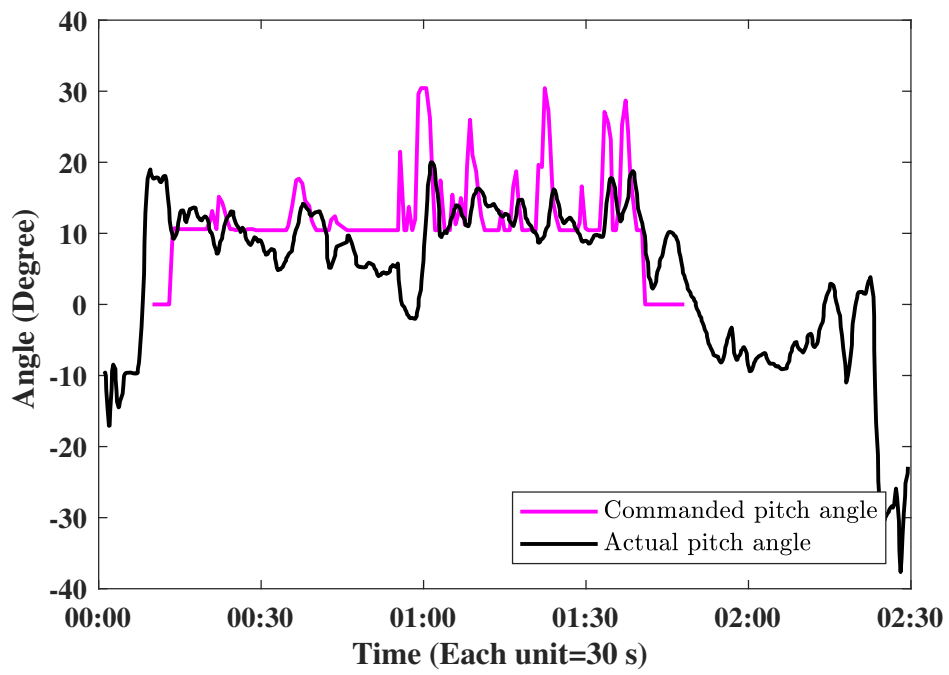


Fig. 24. Commanded pitch angle vs Actual pitch angle

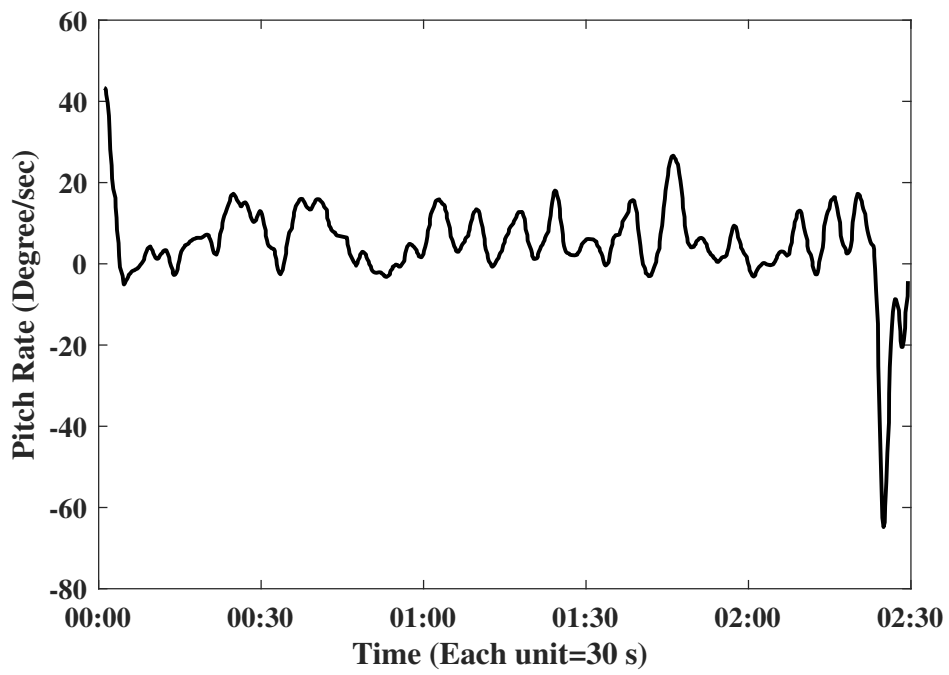


Fig. 25. Pitch rate

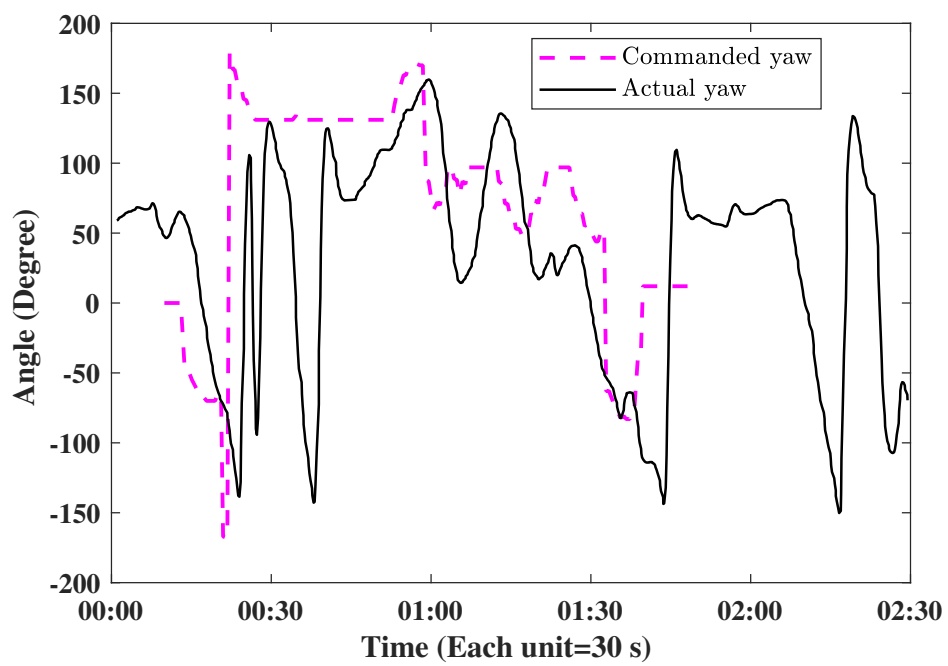


Fig. 26. Commanded yaw angle vs Actual yaw angle

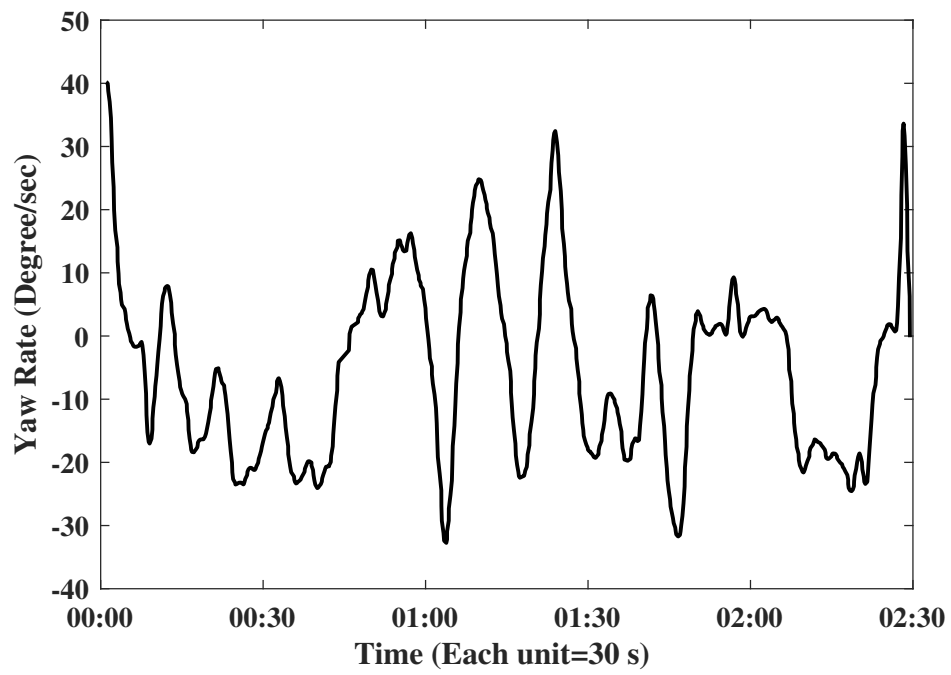


Fig. 27. Yaw rate